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(54) **System for creating a high resolution image from a sequence of lower resolution motion images**

(57) A system for creating a high resolution image from a sequence of lower resolution motion images produces a mapping transformation for each low resolution image to map pixels in each low resolution image into locations in the high resolution image. A combined point

spread function (PSF) is computed for each pixel in each lower resolution image employing the mapping transformations. The high resolution image is generated from the lower resolution images employing the combined PSF's by projection onto convex sets (POCS).

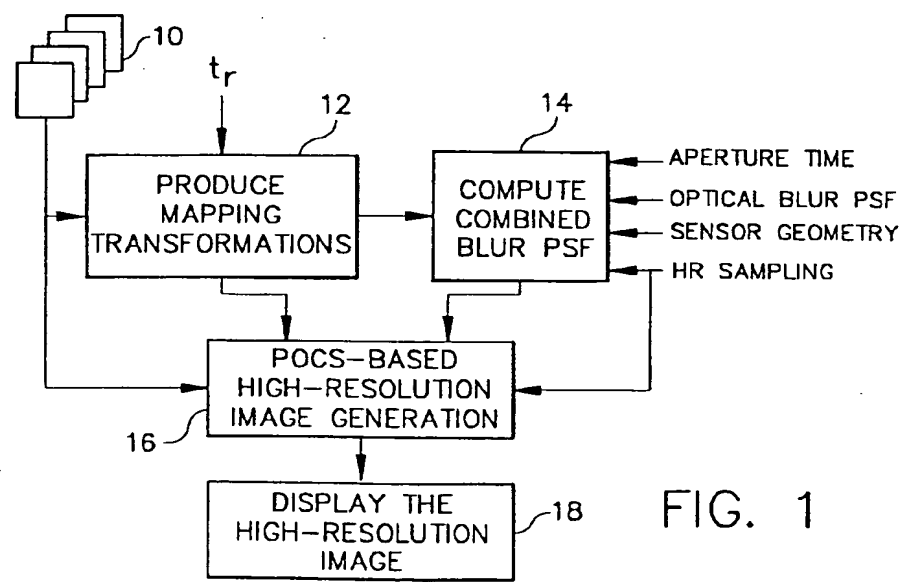


FIG. 1

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**Description****Field of Invention**

5 The present invention is related to the field of digital image processing, and more specifically to a technique for obtaining a high-resolution still image from a sequence of motion images that are of lower resolution, suffering from blur and noise, and under-sampled over an arbitrary lattice.

**Background of The Invention**

10 The present invention relates to a method and apparatus for reconstructing a high-resolution still images from multiple motion images (i.e., images containing relative displacement) that are under-sampled over an arbitrary spatiotemporal lattice and may suffer from blur and noise degradation. The lower-resolution, degraded, multiple motion images may be a series of still images of a particular scene, acquired by an electronic still camera operating sequentially in time, or may be frames digitized from a video signal.

15 Such images are usually undersampled over a sparse spatial lattice (i.e., sampling lattice) due to the presence of a color filter array that samples color channels over a sparse set of points, and/or due to interlacing. In addition, such images suffer from blur and noise. The blur may be due to sensor integration, and/or relative motion between the scene and the camera, and/or nonzero aperture time, and/or camera optics such as defocused lenses. The imaging sensor, and the digitization and quantization processes introduce noise. We refer to images that suffer from one or more of these effects as lower resolution images.

20 Given a multitude of lower resolution images, it is often desirable to create a still image that is of higher quality, for various purposes, such as creating a good quality hard copy print. The resulting still image should have a larger number of samples, preferably over a regular rectangular lattice that is denser than that of the given images, to reduce aliasing effects, and should be free of the effects of blur and noise.

25 In US 5,341,174, Xue et al., describe a method, where the resulting image is obtained by mapping samples from neighboring images onto a selected image, on the basis of relative motion information, in order to increase the number and density of its samples. This approach is limited to interlaced video and does not account for blur and noise degradations. If the data is degraded by blur and/or noise, it is used as it is.

30 Blur due to the integration at the sensor is accounted for in producing a still image in methods discussed in M. Irani and S. Peleg, "Motion analysis for image enhancement: resolution, occlusion, and transparency," J. of Visual Comm. and Image Representation, Vol. 4, pp. 324-335, December 1993.; S. Mann and R. Picard, "Virtual bellows: Constructing high-quality stills from video," in IEEE Int. Conf. Image Proc., (Austin, TX), November 1994.; M. Irani and S. Peleg, "Improving resolution by image registration," CVGIP: Graphical Models and Image Processing, vol. 53, pp. 231-239, May 1991. These methods, however, do not account for the aperture time, and hence do not properly handle the motion blur. Furthermore, they do not model, and hence do not account for, the noise degradation. Consequently, the still images created by these methods may still suffer from motion blur and noise degradation. Furthermore, these methods assume that the input lower resolution images are sampled over a regular, rectangular lattice. If the input images are obtained from an interlaced video, for instance, they should first be deinterlaced (i.e., converted to progressive images sampled over a regular rectangular lattice) prior to the application of the method. Otherwise, the methods are limited to non-interlaced, progressive input images.

40 The method of HIGH RESOLUTION reconstruction discussed in A. M. Tekalp et. al., "High-resolution image reconstruction from lower-resolution image sequences and space-varying image restoration," in IEEE Int. Conf. Acoust., Speech, and Signal Proc., (San Francisco, CA), vol. III, pp. 169-172, March 1992. have used a projections onto convex sets (POCS) based method that accounts for blur due to sensor integration and noise. It does not however account for motion blur, and is applied to non-interlaced, progressive input images only.

**Summary of Invention**

50 One of the objects of this invention is to provide a method for addressing the effects of all above mentioned degradations, namely aliasing (due to spatial undersampling over an arbitrary lattice), sensor blur (due to spatial integration at the sensor, and temporal integration during the aperture time in the presence of relative scene-sensor motion), optical blur (due to defocused lenses), and noise (sensor and quantization noise), in creating a high-quality still image.

55 Another one of the objects of this invention is to provide a complete solution to simultaneous modeling and removal of the effects of aliasing, blurring due to sensor integration, optics, motion, and contamination due to noise. It can therefore create a high resolution still image, or a sequence. Still another object is to reconstruct a high-resolution image from lower resolution images that are sampled over an arbitrary sampling lattice, by reducing the effects of aliasing, by way of increasing the sampling density, and reducing the effects of blurring due to sensor integration and

noise contamination. Yet another object of the present invention is to reconstruct a high-resolution image from lower resolution images that are sampled over an arbitrary sampling lattice, by reducing the effects of aliasing, by way of increasing the sampling density, and reducing the effect of blurring due to sensor integration.

Another object of the invention is to provide a method that can be utilized in a digital still image camera equipped with a high-resolution mode. The high-resolution mode works by invoking a "burst" mode, in which successive images with relative motion are rapidly acquired, and then processed according to the method using either in-camera hardware, or off-line software/hardware processing capabilities, to produce a high resolution still image. Alternatively, successive images containing relative motion can be acquired using an ordinary electronic still camera. One other object of the invention is to provide a method that can be utilized to process images that are acquired by a video camera. Images are processed according to the present invention using either in-camera hardware, or off-line software/hardware processing capabilities, to produce a high resolution still image. The high resolution image is spatially sampled with higher density than is intrinsic to the color filter array (CFA) detector and is non-interlaced. Such a camera is useful, for example, in a desktop video conference system in instances where transmission of very high resolution still images of text, drawings, or pictures is desired.

The objects are achieved according to the present invention by providing a system for creating a high resolution image from a sequence of lower resolution motion images produces a mapping transformation for each low resolution image to map pixels in each low resolution image into locations in the high resolution image. A combined point spread function (PSF) is computed for each pixel in each lower resolution image employing the mapping transformations. The high resolution image is generated from the lower resolution images employing the combined PSF's by projection onto convex sets (POCS).

According to a first embodiment, the step of producing a mapping transformation includes:

- a. selecting one of the lower resolution images as a reference image;
- b. estimating a mapping transformation describing the relative motion at each pixel between the reference lower resolution image and each other lower resolution image;
- c. testing the validity of the estimated mapping transformation for each other lower resolution image pixel and flagging valid mapping transformations; and
- d. scaling each valid mapping transformation from the lower resolution images to the high resolution image.

Advantageously, the step of computing a combined PSF includes:

- a. calculating an effective sampling aperture relative to the high resolution image for each pixel in each lower resolution image employing the mapping transformations;
- b. calculating PSF's for the effective sampling apertures;
- c. defining an optical PSF; and
- d. combining the calculated PSF for each pixel with the optical PSF to produce the combined PSF for each pixel.

As an example, the step of generating the high resolution image by POCS includes:

- a. interpolating one of the lower resolution images to the number of pixels in the high resolution image to produce an estimate of the high resolution image; and
- b. for each pixel in each low resolution image having a valid mapping transformation, refining the estimate of the high resolution image by,

- i. selecting a pixel in one of the lower resolution images,
- ii. producing a calculated pixel value from the high resolution image by applying the combined PSF for the selected pixel to the current estimate of the high resolution image, and
- iii. forming the difference between the selected pixel value and the calculated pixel value and if the magnitude of the difference is greater than a predetermined threshold, back projecting the error into the current estimate of the high resolution image;

- c. clipping the pixel values of the refined estimate of the high resolution image to an allowable range; and
- d. repeating steps b and c until a stopping criterion is satisfied.

Advantageously, a high resolution video sequence from a sequence of lower resolution video images, comprising applying the method of the invention a plurality of times to the sequence of lower resolution video images to produce a video sequence of high resolution images.

The present invention has the advantage that it is capable of processing images that are sampled over an arbitrary

lattice without the need for a preprocessing step where the input has to be interpolated over a regular rectangular lattice unless it is readily sampled over a regular rectangular lattice. The invention uses the method of projections onto convex sets (POCS) in developing a reconstruction method which is amenable to simultaneous handling of blur, noise, and images sampled over arbitrary lattices. The present invention also allows for flexibility in dealing with motion estimates. It allows for a high resolution image reconstruction that is adaptive to the accuracy of motion estimation, as will be described in the following Section.

#### **Brief Description of Drawings**

Figure 1 is a block diagram illustrating the major steps of the invention;

Figure 2 is a diagram showing lower resolution sampling lattices and the sampling lattice of the high resolution image according to the present invention;

Figure 3 is a schematic diagram depicting a system suitable for implementing the present invention;

Figure 4 is a diagram illustrating a sequence of lower resolution images and a selected region of interest within one of the lower resolution images;

Figures 5 and 6 are diagrams useful in describing the method of producing a mapping transformation according to the present invention;

Figure 7 is a block diagram illustrating the image formation model used for calculating the combined PSF according to the present invention;

Figure 8 is a diagram illustrating the effective transformation of the blur PSF due to relative motion between lower resolution images in the sequence;

Figure 9 is a diagram useful in describing the PSF for the case of translational motion;

Figure 10 is a diagram depicting the procedure for computing the LSI blur function  $h_2(x_1, x_2, t, t_r)$ ;

Figure 11 is a diagram useful in describing the segmentation of  $h_2(x_1, x_2, t, t_r)$  into regions;

Figure 12 is a diagram useful for describing the approximation used for affine and perspective motion models in computing the combined effective blur PSF; and

Figure 13. is a diagram useful in describing the POCS-based reconstruction method.

#### **Detailed Description of Invention**

The major steps of the present invention are depicted in the flow diagram shown in Fig. 1, where a number of lower resolution motion images 10 are presented as the input to the image processing method. One of the input images is selected, by a user, from the input set of lower resolution images 10. This image is referred to as the reference image and it is that image whose high resolution version will be reconstructed. The reference image is specified by its time index  $t_r$ .

The present invention has three major processing steps. In referring to Fig. 1, the first processing step 12 provides mapping transformations that map the pixels in each lower resolution input image into locations in the high resolution image. To produce the mapping transformations, a motion vector field is estimated for each pixel in each one of the other lower resolution images relative to the lower resolution reference image. A motion estimation method, such as the well-known hierarchical block matching method with fractional pixel accuracy, can be used. Alternatively, the motion estimation method disclosed in U.S. patent No. 5,241,608 issued Aug. 31, 1993 to Fogel may be employed to estimate the motion vector field. The block matching method is based on a locally translational motion model. Another possibility is to use affine motion models, as will be described later on, that model zoom, rotation and shear in addition to translation, within a region.

The second processing step 14 uses the mapping transformation information, made available by the preceding step 12, aperture time, sensor geometry, optical blur point spread function (PSF), and the high resolution sampling geometry (HR) to compute the combined blur PSF that accounts for the motion and optical blur, and blur due to integration

at the sensor. Computation of the combined blur PSF is based on an image formation model that is described below.

The high resolution image is created in the third step 16 where the combined blur PSF, the motion information from the mapping transformations, and the given lower resolution images 10 are used in a method based on POCS, described in detail in the article by M.I. Sezan, "An overview of convex projections theory and its applications to image recovery problems," Ultramicroscopy, no. 40, pp. 55-67, 1992. The high resolution image reconstructed at this final step is an estimate of the high resolution version of the reference image that has a larger number of samples over a denser, regular rectangular sampling geometry (HR), regardless of the sampling lattice pattern of the input lower resolution images, and is free from blur and noise degradation. Finally, the high resolution image is displayed 18 on a display device such as a CRT or a printer.

The lower resolution images may be sampled with different sampling patterns at different times. When this happens, a sampling lattice describes the periodic change in the sampling patterns. Typical sampling lattice patterns for lower resolution, and the high resolution image are depicted in Fig. 2. Pattern (a) shows a diamond-shaped lattice, Pattern (c) is an interlaced lattice, and Pattern (b) and (d) show the denser lattice over which the high resolution image is reconstructed. The open circles in the diagram denote the new samples generated by the high resolution reconstruction process, and the solid circles denote the sampling pattern in the lower resolution image. Note that Fig. 2 shows a 2x increase in the effective sampling density. The method of the present invention allows for higher factors of increase, if desired. Note also that one can generate a high resolution sequence by processing not one but all of the lower resolution images in a sequential manner, each time designating one of the images as the reference image. Such a process would be useful for example to produce high resolution video.

Referring to Fig. 3, a system useful in practicing the present invention is shown. Input devices such as a video camcorder/VCR 20 connected to a digitizer 22, a digital still camera 24, a digital video camcorder 26, a digital scanner 28 or a disc storage 30 provide a source of a motion sequence of digital images. The motion sequence of digital images are supplied to an image processing computer system generally 32. The image processing computer system includes a computer 34 such as a Power PC, a CRT display 36 having typically SVGA or better resolution, and an operator input device such as a keyboard 38 or a mouse. The computer 34 is connected to an output device such as a printer 40 for creating a hard copy display of the high resolution image; a storage medium 42 such as an optical disc for storage pending eventual display of the image; or link to a communication network 44 for distributing the high resolution image for remote display.

Once the multiple low resolution images are available to the computer system 32 for display on CRT 36, it is also possible for a user to interactively specify a region of interest in the reference image and confine the resolution improvement process to that region. Fig. 4 shows a sequence of low resolution images 46, 48 and 50, where region of interest 52 in image 48 has been identified for high resolution processing. In this case, the high resolution version of the selected region is reconstructed over a high resolution sampling geometry, and the result is then down-sampled over the lattice of the lower resolution image and then placed into the region of interest replacing the values of the original pixels. In the depiction in Fig. 4, the face of the person forms the region of interest 52; In the resulting image, the facial detail will be available at high resolution. The user may visually identify regions that correspond to the selected region of interest 52. Then the process is applied only to these regions, rather than to the entire lower resolution images, resulting in computational savings.

#### A. Mapping Transformation

Motion is estimated from the each one of the lower resolution images to the reference image, resulting in M-1 motion vector fields for M lower resolution images to provide a mapping transformations that map lower resolution image pixels to the high resolution image sampling locations. This is graphically depicted in Fig. 5. In the simplest case, the motion from the lower resolution image 46 to the reference image 48 can be modeled as a spatially uniform translation. In practice, however, we have found this model to be sub-optimal. The hierarchical block matching method, to estimate non-uniform translational motion, and methods based on affine models and estimators are more effectively used to estimate the motion vector fields.

The lower resolution images 46, 48, 50, 53 are first bilinearly interpolated over a rectangular lower resolution lattice, for the purpose of motion estimation, unless they are already available over a rectangular lattice. For example, a diamond-shaped lower resolution input lattice 54 and the corresponding lower resolution rectangular lattice 56 are depicted in Fig. 6. The interpolated values of the reference image are only used for motion estimation and subsequently discarded and replaced with the estimates during the POCS-based high resolution reconstruction process. A motion vector is estimated for each actual pixel of the lower resolution images, resulting in M-1 motion vector field estimates.

In the case of a block matching method of motion estimation, the motion is assumed to be locally translational. When other transformation effects are small, this approximation can be quite effective. The hierarchical block matching method (HBM) discussed in M.Bierling, "Displacement estimation by hierarchical block matching," in Proc. SPIE Visual Communications and Image Processing '88, pp. 942-951, 1988 is used to estimate the non-uniform motion field. The

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matching criterion used is the mean absolute difference (MAD) between measurement blocks. At each level in the hierarchy, a logarithmic type search is used.

The preferred parameter values that can be used in the implementation of a 5-level HBM are furnished in Table 1, where the first column is the hierarchy level number, and level 1 is the lowest resolution level.

Table 1

Level	Max Displ.		Window Siz		Filter Size		Step Size	SSF	Accurac
	hor.	vert.	hor.	vert.	hor.	vert.			
1	31	31	128	128	10	10	32	8	1
2	15	15	64	64	10	10	16	8	1
3	7	7	64	64	5	5	8	4	1
4	3	3	28	28	5	5	4	4	1
5	1	1	12	12	3	3	3	2	0.25

The maximum horizontal/vertical displacement (Max Disp. hor./vert.) is the displacement used in the first step of the logarithmic search. The horizontal/vertical measurement window size (Window Size hor./vert.) is the size of the window over which the MAD is computed. The horizontal/vertical filter size (Filter Size hor./vert.) specifies the support of a Gaussian filter, with variance set to 1/2 of the support size. The step size is the horizontal and vertical distance between neighboring pixels in the reference image for which an estimate of the motion is computed, the subsampling factor (SSF) is the horizontal and vertical subsampling used when computing the MAD over the measurement window, and the accuracy of estimation is in terms of the sampling period of the lower resolution rectangular lattice. Note that all units for the parameters are relative to the spatial sampling period of the lower resolution rectangular lattice (i.e., refinement to 1/4 - pixel accuracy, relative to the lower resolution rectangular lattice, is performed in the final level of HBM).

Significant non-translational mapping transformations (resulting from rotations, shears and zooms) cannot be accurately modeled using the block matching techniques described above. It is preferable to model inter-image motion resulting in such mapping transformations using a global affine transformation defined by the parameters  $c_1$ - $c_6$  in the following equation:

$$g(x_1 + c_1 + c_2 x_1 + c_3 x_2, x_2 + c_4 + c_5 x_1 + c_6 x_2, t) = g(x_1, x_2, t) \quad (1)$$

The technique that can be used to estimate the parameters  $c_1$ ,  $c_2$ ,  $c_6$  is described in J. Bergen, P. Burt, R. Hingorani, and S. Peleg, "A three-frame algorithm for estimating two-component image motion," IEEE Trans. Pattern Anal. Intel., vol. 14, pp. 886-896, September 1992. This estimation method requires spatial and temporal derivatives to be estimated. The spatial derivatives are estimated using a 2-D second-order polynomial least-squares fit over a 5x5 window centered at each pixel, while the temporal derivatives are computed using a 2-point finite forward difference at each pixel. Prior to estimating these derivatives, the images are blurred using an 11x11 pixel uniform blur to reduce the effects of noise.

In case of color imagery, motion is estimated in the luminance domain. The same motion information is then used in separately processing the primary color channels (e.g., red, green, and blue) of the given lower resolution images. Therefore, an RGB to luminance and two chroma (e.g., YUV) transformation is applied to the lower resolution images prior to motion estimation for forming the mapping transformations.

## B. Modeling and Computing The Combined PSF

Computation of the combined PSF is based on an image formation and blur model. In the following we describe this model that is then used in computing the combined PSF.

We first describe a model that relates the given lower resolution images, to the actual high resolution image, at a particular reference time  $t_r$ , through a continuous linear shift variant (LSV) blurring relationship. Towards this end, first, an image formation model is described. The mapping transformations are then incorporated into the formation model, resulting in the desired LSV relationship expressed in terms of a combined blur PSF. Next, a discretization is presented to relate a discrete version of the high resolution image to the observed lower resolution imagery, by means of a corresponding discrete LSV relationship, expressed in terms of a discrete combined blur PSF. Finally, a practical method is provided to compute the combined PSF for subsequent reconstruction of the high resolution image.

Image Formation Model

The image formation model we use is depicted in Fig. 7. In the figure, the input signal  $f(x_1, x_2, t)$  denotes the actual high resolution imagery in the continuous domain, whose discrete estimate is desired. The effects of the physical dimensions of the lower resolution sensor, i.e., blur due to integration over the sensor area, and the blur of the optical system are modeled in the first stage 60 of the figure. The high resolution imagery  $f(x_1, x_2, t)$  is convolved with both the kernel representing the shape of the sensor  $h_a(x_1, x_2, t)$ , and the optical blur kernel  $h_o(x_1, x_2, t)$ . These are both functions of time, but we restrict them to be constant over the aperture time. The optical blur and aperture dimensions are thus allowed to differ from image to image.

The effect of aperture time is modeled in the second stage 62 of Fig. 7 by a time-domain integrator whose output is given by

$$g_2(x_1, x_2, t) = \frac{1}{T_a} \int_{t-T_a}^t g_1(x_1, x_2, \tau) d\tau, \quad (2)$$

where  $T_a$  denotes the sensor aperture time. Note that the first two stages 60 and 62 commute, since the first is spatially linear shift-invariant (LSI) and the second is temporally LSI.

The third stage 64 in Fig. 7 models low resolution sampling using the arbitrary space-time lattice  $\Lambda_s$ . The output of this stage is denoted by  $g_2(m_1, m_2, k)$ . As a matter of convention, integer values  $m_1$ ,  $m_2$ , and  $k$ , that appear as a function argument, are interpreted as in

$$g_2(m_1, m_2, k) = g_2(x_1, x_2, t) \Big|_{[x_1 x_2 t]^T = V_s [m_1 m_2 k]^T} \quad (3)$$

where  $V_s$  denotes the matrix that specifies the sampling lattice, and  $^T$  denotes the transpose operation. In the last modeling step 66, additive noise due to the lower resolution sensor is added to the sampled video signal.

Including Motion

We now incorporate a motion model into the image formation model to establish the desired LSV relationship between the lower resolution imagery and the desired high resolution image at a fixed but arbitrary time instance  $t_r$ . By appropriately setting the value(s) of  $t_r$ , a single still high resolution image, or high resolution video images, comprised of a sequence of high resolution images, can be reconstructed.

When a motion model is applied to the image formation model, the first two stages 60 and 62 in Fig. 7 can be combined to form a single LSV relation. We begin by considering motion as in

$$f(x, t) = f(M(x, t, t_r), t_r) = f(x_r, t_r), \quad (4)$$

where  $x$  denotes  $(x_1, x_2)$ , and  $M(x, t, t_r)$  is a mapping transformation relating the position of an intensity at position  $x$  and time  $t$ , to its position at time  $t_r$ . This equation expresses the well-known assumption of intensity conservation along motion trajectories. By letting  $h_1(x, t) = h_a(x, t) * h_o(x, t)$ , the output of the first modeling stage can be expressed as

$$g_1(x, t) = \int h_1(x - \chi) f(\chi, t) d\chi \quad (5)$$

By making the change of variables  $x_r = M(x, t, t_r)$  and using (4), (5) becomes

$$g_1(x, t) = \int h_1(x - M^{-1}(x_r, t, t_r)) f(x_r, t_r) |J(M)|^{-1} dx_r \quad (6)$$

where,  $M^{-1}$  denotes the inverse transformation,  $J(M)$  denotes the Jacobean of  $M$ , and  $|J(M)|$  denotes the determinant operator. It is evident from (6) that the first stage of the model has been transformed into an LSV operation, acting on a high resolution image at time  $t_r$ . To reflect this fact, we let

$$h_1(x, x_r, t, t_r) = h_1(x - M^{-1}(x_r, t, t_r)) |J(M)|^{-1} \quad (7)$$

denote the combined LSV blur point spread function (PSF) modeling the effect of the sensor geometry, optical blur, and relative motion. The effect of this equation is depicted in Fig. 8, where the picture at the left depicts the imaging process at time  $t$ , where the aperture 68 of a sensor element is imposed on the picture. The picture to the right shows

the equivalent imaging process at time  $t_r$ . Notice the mapping transformation applied to the aperture 68 in going from time  $t$  to  $t_r$  is the inverse of the mapping transformation applied to the image 70. Rewriting (6) in LSV form yields

$$g_1(x, t) = \int h_1(x; x_{t_r}; t, t_r) f(x_{t_r}, t_r) dx_{t_r} \quad (8)$$

The second modeling stage can now be expressed as

$$g_2(x, t) = \int_{t-T_a}^t h_1(x; x_{t_r}; \tau, t_r) f(x_{t_r}, t_r) dx_{t_r} d\tau \quad (9)$$

By changing the order of the integrations, the above becomes

$$g_2(x, t) = \int h_2(x; x_{t_r}; t, t_r) f(x_{t_r}, t_r) dx_{t_r} \quad (10)$$

where,

$$h_2(x; x_{t_r}; t, t_r) = \int_{t-T_a}^t h_1(x; x_{t_r}; \tau, t_r) d\tau \quad (11)$$

Thus the first two stages of the model have been combined into a single LSV system, acting on the continuous high resolution image at time  $t_r$ . This allows us to write the observed lower resolution imagery in terms of a continuous high resolution image at time  $t_r$ , as

$$g(m_1, m_2, k) = \int h_2(m_1, m_2; x_{t_r}; k, t_r) f(x_{t_r}, t_r) dx_{t_r} + v(m_1, m_2, k). \quad (12)$$

where  $h_2(*)$  is the effective LSV blur PSF, and the integer arguments  $m_1$ ,  $m_2$ , and  $k$  have the same interpretation as in (3).

#### Discretization

It is desirable to discretize the LSV blur relationship in (12), to relate the observed lower resolution images to a discrete version of the actual high resolution image  $f(x_1, x_2, t_r)$ . Thus, a discrete superposition summation of the form

$$g(m_1, m_2, k) = \sum_{(n_1, n_2)} f(n_1, n_2, t_r) h_{t_r}(n_1, n_2; m_1, m_2, k) + v(m_1, m_2, k), \quad (13)$$

will now be formulated. We assume that the continuous imagery  $f(x_1, x_2, t_r)$  is sampled on the 2-D lattice  $\Lambda_{t_r}$  i.e.  $(n_1, n_2)$  are integers that specify a point in  $\Lambda_{t_r}$ , by a high resolution sensor, to form  $f(n_1, n_2, t_r)$ . By appropriately choosing  $t_r$  and  $\Lambda_{t_r}$ , sampling of  $f(n_1, n_2, t_r)$  can be formed over an arbitrary space-time lattice.

An individual high resolution sensor element (giving rise to a single high resolution image pixel) is assumed to have physical dimensions which can be used as a unit cell  $U_{t_r}$  for the lattice  $\Lambda_{t_r}$ . Thus, the entire space of the focal plane is completely covered by the high resolution sensor. The term  $U_{t_r}(n_1, n_2)$  is used to denote the unit cell  $U_{t_r}$  shifted to the location specified by  $(n_1, n_2)$ . With this definition, and with the assumption that  $f(x_1, x_2, t_r)$  is approximately constant over  $U_{t_r}(n_1, n_2)$ , (12) can be written as

$$g(m_1, m_2, k) = \sum_{(n_1, n_2)} f(n_1, n_2, t_r) \int_{U_{t_r}(n_1, n_2)} h_2(m_1, m_2; x_{t_r}; k, t_r) dx_{t_r} + u(m_1, m_2, k). \quad (14)$$

By comparing (13) with (14), it is evident that

$$h_{t_r}(n_1, n_2; m_1, m_2, k) = \int_{U_{t_r}(n_1, n_2)} h_2(m_1, m_2; x_{t_r}; k, t_r) dx_{t_r}, \quad (15)$$

where the integer arguments  $m_1$ ,  $m_2$ ,  $k$ ,  $n_1$ , and  $n_2$  are interpreted as in (3).



A pictorial example of the discrete LSV PSF formulation, with a rectangular high resolution lattice  $\Lambda_{tr}$ , is provided in Fig. 9. In the figure, it is assumed that the motion is purely translational, that a square lower resolution sensor aperture 68 centered on a point  $(m_1, m_2)$  73 is used, and that there is no optical blur. The  $(x_1, x_2)$  space is the sensor focal plane at time  $t_r$ . The focal plane is shown covered by shifted high resolution sampling unit cells  $U_{tr}(n_1, n_2)$  69. The region of the focal plane "swept" by the lower resolution sensor aperture 68 during the aperture time  $T_a$  is shown by dotted outline 71. The discrete LSV PSF specified in (15) is formed by computing the duration of time a given area of the lower resolution sensor 68 "dwelled" over a region  $U_{tr}(n_1, n_2)$  69, while translating from its position at the aperture opening time, to its position 73 at the aperture closing time. Note that the result indicated by (15) does not specify a simple area of overlap between the area 71 swept by sensor aperture 68 and the high resolution sampling regions  $U_{tr}(n_1, n_2)$  69.

#### Computation of the Combined PSF

A practical method for computing the blur function  $h_{tr}(\cdot)$  given by (15) is described. Two cases will be treated to serve this goal. In the first case, translational motion is assumed. In the second case, general image motion is considered. To solve this second case, a general approximation is given, that leads to a blur computation method that is built on top of the method delineated for the translational motion case. Relative to this approximation, we provide specific methods for affine and perspective transformation models of motion.

##### 1) Translational motion.

For the case of translational motion, we define piece wise constant velocity motion paths, effective during the  $k^{\text{th}}$  opening of the aperture (i.e. acquiring the  $k^{\text{th}}$  lower resolution image at time  $t_k$ ), as

$$x_{tr} = M(x, t, t_r) = x + x_{bk} + v_k(t - (t_k - T_a)), \quad (16)$$

where the velocities  $v_{1,k}$  and  $v_{2,k}$ , where  $v_k = [v_{1,k} \ v_{2,k}]^T$ , are assumed to be constant over the aperture time  $T_a$ ,  $(t_k - T_a)$  is the time of the  $k^{\text{th}}$  opening of the aperture, and  $x_{bk}$  denotes the relative initial position at the  $k^{\text{th}}$  opening of the aperture. The quantity  $x_{bk}$  is a function of the times  $t_k$  and  $t_r$ . If for the moment the optical blur is ignored, then the PSF

$$h_2(x, x_{tr}; t, t_r)$$

is LSI, and by defining

$$h'_2(x - x_{tr}; t, t_r) = h_2(x, x_{tr}; t, t_r)$$

and applying (7) and (11)

$$h'_2(x, t, t_r) = \frac{1}{T_a} \int_0^{T_a} h_a(x + x_{bk} + v_k \tau) d\tau \quad (17)$$

If we now assume the aperture response is a 2-D "rect" function given by

$$h_a(x_1, x_2) = \begin{cases} \frac{1}{\Delta M_1 \Delta M_2}; & -\frac{\Delta M_1}{2} < x_1 < \frac{\Delta M_1}{2} \text{ and } -\frac{\Delta M_2}{2} < x_2 < \frac{\Delta M_2}{2} \\ 0; & \text{else,} \end{cases}$$

then  $h'_2$  can be computed graphically as depicted in Fig. 10. The coordinate  $x + x_{bk}$  sets the starting point 76 of the line 78 shown in the figure, at time  $\tau=0$ . The integral follows the line 78 to its endpoint 80 at  $\tau=T_a$ , and the result is simply the length of the line segment 78 that intersects the aperture 68.

To further describe the blur  $h'_2$ , consider the case where  $v_{1,k}T_a > \Delta M_1$  and  $v_{2,k}T_a > \Delta M_2$ . The point spread function  $h'_2(x - x_{bk})$  (the shift is used for convenience) can then be segmented into regions within the  $(x_1, x_2)$  plane, as shown in Fig. 11. In each of the 7 regions depicted in the figure, the value of  $h'_2(x - x_{bk})$  is described by a linear equation in  $x_1$  and  $x_2$ . For instance, in the region marked with the number 1, which is a parallelogram, the value of  $h'_2$  is constant. In the trapezoidal region marked with a 2,  $h'_2$  is found using the equation

$$h'_2(x_1 - x_{1,bk}, x_2 - x_{2,bk}) = \quad (18)$$

$$K \left( \left( v_{2,k} \left( x_1 + \frac{\Delta M_1}{2} + v_{1,k} T_a \right) \right) - v_{1,k} \left( x_2 - \left( \frac{\Delta M_2}{2} - v_{2,k} T_a \right) \right) \right), \quad (19)$$

for all

$$(x_1, x_2)$$

within Region 2,

where K is a scaling constant that can be accounted for by normalizing the discrete PSF  $h_{ir}$ .

The discrete PSF  $h_{ir}$  (15) is computed by integrating over the volume under the region

$$U_{ir}(n_1, n_2)$$

69 shown in Fig. 11. The center 82 of this region 69 is located at

$$x = x_s(m_1, m_2, k) + x_{bk} - x_{ir}(n_1, n_2),$$

where

$$x_{ir}(n_1, n_2)$$

is defined similarly to

$$x_s(m_1, m_2, k).$$

Thus,

$$h_{ir}(x_1 - x_{1,bk}, x_2 - x_{2,bk})$$

is computed by finding the volume under

$$h'_2(x_1 - x_{1,bk}, x_2 - x_{2,bk}),$$

in the region 69, whose position is determined by  $(m_1, m_2)$  and  $(n_1, n_2)$ .

The optical blur  $h_o(x, t)$  can be subsequently taken into account using a discrete approximation by carrying out the convolution

$$h_{ir}(n_1, n_2; m_1, m_2, k) **_{n_1, n_2} h_{ok}^d(n_1, n_2) \quad (20)$$

where

$$h_{ok}^d(n_1, n_2)$$

is the discrete representation of the focus blur for the  $k^{\text{th}}$  lower resolution image, and  $**_{n_1, n_2}$  denotes 2-D discrete convolution over the variables  $(n_1, n_2)$ . By taking the optical blur into account in this way, we are making the assumption that the blur PSF  $h_{ir}$ , within a region about  $x_s(m_1, m_2, k)$ , is approximately LSI. This is a reasonable assumption as long as the image has not undergone an extreme non-translational motion. Handling the optical blur as in (20) is attractive, since  $h_{ir}$  can easily be computed when the optical blur is not considered, and the convolution in (20) is easy to implement. In a preferred implementation, the optical blur PSF is set equal to a Gaussian with unity variance and with 5x5 pixel support, expressed in terms of high resolution sampling lattice.

## 2) General motion.

We now extend this method for computing the blur to the case of more complex motions, such as those described by affine or perspective transformations. The extension is based on the following observation: the transformation due to motion between the times  $t_r$  and  $t_k$  may be significant, however, the non-translational component of the transformation that effects the blur shape will be small during the aperture time. This concept is demonstrated in Fig. 12. The

figure is a graphical representation of the computation described in (11), which is rewritten here as

$$h_2(x; x_{t_r}, t, t_r) = \int_{t-T_a}^t h_1(x - M^{-1}(x_{t_r}, \tau, t_r)) \left| J(M(x_{t_r}, \tau, t_r)) \right|^{-1} d\tau \quad (21)$$

The figure depicts the transformed blur kernel  $h_1(\cdot)$  as it translates across the plane  $x_t$  during the integration time, from  $t-T_a$  84 to  $t$  86. The value of  $h_2(\cdot)$  is then the "dwell" time over  $x_{t_r}$  weighted by the Jacobian and the amplitude of  $h_1(\cdot)$ . Computation of (21) is difficult since the translating kernel  $h_1$  in (21) is continuously transforming during the integration period. As previously pointed out, however, the non-translational component of this transformation, during the aperture time, is assumed to be small. This effect is demonstrated in Fig. 12 by showing the dotted outline of the function

$$h_1(M^{-1}(x_{t_r}, t - T_a, t_r))$$

84 superimposed on

$$h_1(M^{-1}(x_{t_r}, t, t_r))$$

86. In terms of (21), the approximation makes the assumptions that: (i) the Jacobean weighting is a constant, (ii) the transformation

$$M(x_{t_r}, \tau - T_a, t_r)$$

is maintained throughout the aperture time (i.e., this function only translates as  $\tau$  changes), and (iii) the path of translation during two consecutive frames, and thus within the aperture time, is linear. With this approximation, (21) can be rewritten as

$$\left| J(M(x, t - T_a, t_r), \tau, t_r) \right|^{-1} \int_{t-T_a}^t h_1(\ell(x, \tau) - M^{-1}(x_{t_r}, t - T_a, t_r)) d\tau \quad (22)$$

where,

$$\ell(x, \tau) = \frac{T - \tau}{T} x + \frac{\tau}{T} M^{-1}(M(x, t - T_a + t, t_r), t - T_a, t_r) \quad (23)$$

and  $T$  is the time between consecutive frames.

Using this approximation, the same procedure for computing the blur in the case of spatially uniform, temporally piece wise constant-velocity translational motion is used, except that at each point  $x$  the blur is computed with the appropriate transformation applied to the rectangular function 68 depicted in Fig. 10. To summarize, when the transformation is defined by uniform and constant translations, the approximation will result in an exact blur computation. When the transformation is affine, the Jacobean does not vary with  $x_{t_r}$ , but we have approximated it to be constant over time, while the aperture is open. Additionally, the translation is assumed to be constant-velocity, where this may not necessarily be the case. In the case of perspective motion, the approximation has the same effects as in the affine case, with the additional approximation that the Jacobean is constant over the spatial blur support of  $h_1(\cdot)$ .

### C. Reconstruction of The High Resolution Image

Given the combined blur PSF,  $h_{t_r}$ , the motion vector field estimates from lower resolution images to the reference image, and the high resolution sampling lattice, the high resolution image is reconstructed using the following technique based on the method of POCS. In POCS, the desired image distribution is assumed to be a member of a mathematical vector space, such as the  $P$ -dimensional vector space, for a  $N_1$  pixels by  $N_2$  lines ( $P = N_1 \times N_2$ ) high resolution image. The method of POCS requires the definition of closed convex constraint sets within this vector space, that contain the actual high resolution image. Mathematical intersection of these sets contain the actual high resolution image since it is contained in each one of them. An estimate of the actual high resolution image is then defined as a point in the intersection of these constraint sets, and is determined by successively projecting an arbitrary initial estimate onto the constraint sets, as is well known in the literature.

Associated with each constraint set is a projection operator  $P$ , mapping an arbitrary point within the space, but

outside the set, to the closest point within the set. Relaxed projection operators,  $T = (1 - \lambda)I + \lambda P$ ,  $0 < \lambda < 2$ , where  $I$  denotes the identity operator, can also be defined and used in finding an estimate in the intersection set.

We now describe how we utilize the principles of POCS in developing a method to solve the high resolution reconstruction problem at hand. We define the following closed, convex constraint set, for each pixel within lower resolution image sequence  $g(m_1, m_2, k)$ :

$$C_{t_r}(m_1, m_2, k) = \left\{ y(n_1, n_2, t_r) : |r^{(y)}(m_1, m_2, k)| \leq \delta_0 \right\}, \quad (24)$$

where

$$r^{(y)}(m_1, m_2, k) = g(m_1, m_2, k) - \sum_{n_1, n_2} y(n_1, n_2, t_r) h_{t_r}(n_1, n_2; m_1, m_2, k), \quad (25)$$

is the residual associated with an arbitrary member,  $y$ , of the constraint set. We refer to these sets as the data consistency constraint sets. The quantity  $\delta_0$  is an *a priori* bound reflecting the statistical confidence with which the actual image is a member of the set  $C_{t_r}(m_1, m_2, k)$ . Since  $r^{(0)}(m_1, m_2, k) = v(m_1, m_2, k)$ , where  $v$  denotes the actual high resolution image, the statistics of  $r^{(0)}(m_1, m_2, k)$  are identical to those of  $v(m_1, m_2, k)$ . Hence the bound  $\delta_0$  is determined from the statistics of the noise process so that the actual image (i.e., the ideal solution) is a member of the set within a certain statistical confidence. For example, if the noise has Gaussian distribution with standard deviation  $\sigma$ ,  $\delta_0$  is set equal to  $c\sigma$ , where  $c\sigma$  is determined by an appropriate statistical confidence bound (e.g.,  $c=3$  for 99% confidence).

It is also possible, in practice, to directly adjust the value of  $\delta_0$ . As  $\delta_0$  increases, the reconstructed image becomes sharper but noisy. As  $\delta_0$  decreases, the resulting reconstruction becomes less noisy but smoother. In our extensive tests, setting  $\delta_0$  equal to 0.01 has resulted in fairly rapid convergence of the POCS method to an image with sufficiently good quality.

Note that the sets  $C_{t_r}(m_1, m_2, k)$  can be defined only those spatial locations where samples of the lower resolution images are available. This enables the invention to be applicable to any arbitrary lower resolution sampling lattice. Further, the sets  $C_{t_r}(m_1, m_2, k)$  can be defined only for those samples of the lower resolution images where there are no occlusions and uncovered regions. The latter fact makes the invention adaptive to changing scenes within a given motion imagery. In short, constraint sets are defined only for appropriate samples of the lower resolution imagery.

The projection  $z(n_1, n_2, t_r)$   $P_{t_r}(m_1, m_2, k) [x(n_1, n_2, t_r)]$  of an arbitrary  $x(n_1, n_2, t_r)$  onto  $C_{t_r}(m_1, m_2, k)$  can be defined as:

$$P_{t_r}(m_1, m_2, k) [x(n_1, n_2, t_r)] = \begin{cases} x(n_1, n_2, t_r) + \frac{(r^{(x)}(m_1, m_2, k) - \delta_0) h_{t_r}(n_1, n_2; m_1, m_2, k)}{\sum_{o_1} \sum_{o_2} h_{t_r}^2(o_1, o_2; m_1, m_2, k)}, & r^{(x)}(m_1, m_2, k) > \delta_0 \\ x(n_1, n_2, t_r), & -\delta_0 \leq r^{(x)}(m_1, m_2, k) \leq \delta_0 \\ x(n_1, n_2, t_r) + \frac{(r^{(x)}(m_1, m_2, k) + \delta_0) h_{t_r}(n_1, n_2; m_1, m_2, k)}{\sum_{o_1} \sum_{o_2} h_{t_r}^2(o_1, o_2; m_1, m_2, k)}, & r^{(x)}(m_1, m_2, k) < -\delta_0 \end{cases} \quad (26)$$

Additional constraints such as bounded energy, positivity, and limited support can be utilized to improve the results. We use the amplitude constraint set,

$$C_A = \{y(n_1, n_2, t_r) : \alpha \leq f(n_1, n_2, t_r) \leq \beta\}, \quad (27)$$

with amplitude bounds of  $\alpha=0$  and  $\beta=255$ . The projection  $P_A$  onto the amplitude constraint set  $C_A$  is defined as

$$P_A[x(n_1, n_2, t_r)] = \begin{cases} 0, & x(n_1, n_2, t_r) < 0 \\ x(n_1, n_2, t_r), & 0 \leq x(n_1, n_2, t_r) \leq 255 \\ 255, & x(n_1, n_2, t_r) > 255 \end{cases} \quad (28)$$

Given the above projections, an estimate,  $\hat{f}(n_1, n_2, t_r)$ , of the high resolution image  $f(n_1, n_2, t_r)$ , is obtained iteratively from all lower resolution images  $g(m_1, m_2, k)$ , where constraint sets can be defined, as

$$\hat{f}_{\ell+1}(n_1, n_2, t_r) = T_A \tilde{T}[\hat{f}_{\ell}(n_1, n_2, t_r)] \quad \ell = 0, 1, 2, \dots \quad (29)$$

where  $\tilde{T}$  denotes a cascade of the relaxed projection operators, projecting onto the family of sets

$$C_{t_r}(m_1, m_2, k).$$

Any lower resolution image, bilinearly interpolated over the high resolution sampling lattice can be used as the initial estimate

$$\hat{f}_0(n_1, n_2, t_r).$$

Choosing the lower resolution image with the best visual quality for initialization may increase the speed of reaching at an iteration number  $\ell$  at which a visually satisfactory high resolution image is reconstructed. In theory, the iterations continue until an estimate lies within the intersection of all the constraint sets. In practice, however, iterations are generally terminated according to a certain stopping criterion, such as visual inspection the image quality, or when changes between successive estimates, as measured by some difference metric (i.e.,

$$\|\hat{f}_{\ell} - \hat{f}_{\ell-1}\|,$$

using the  $L_2$  norm), fall below a preset threshold.

A pictorial depiction of this method is given in Fig. 13. The combined LSV blur relates a region 71 of the current high resolution image 88 estimate, say  $f_{\ell}(\cdot)$ , to a particular pixel intensity  $q(m_1, m_2, k)$  90 in one of the lower resolution images 46, 48, 53. The residual term

$$r^{(\hat{f})}(m_1, m_2, k)$$

is then formed, which indicates whether or not the observation could have been formed from the current high resolution image estimate (within some error bound determined by  $\delta_0$ ), and therefore whether the high resolution estimate belongs to the data consistency set

$$C_{t_r}(m_1, m_2, k).$$

If it is not in the set (i.e. the residual is too large), the projection operator

$$P_{t_r}(m_1, m_2, k)$$

back projects the residual onto the current high resolution image 88 estimate (the additive term in (26)), thus forming a new estimate of the high resolution image that does belong to the set

$$C_{t_r}(m_1, m_2, k),$$

and therefore could have given rise to the observation  $g(m_1, m_2, k)$ , within the bound  $\delta_0$ . Performing these projections over every lower resolution pixel 90 where a consistency constraint set is defined, completes the composite projection

$$\tilde{T}[\hat{f}_{\ell}(n_1, n_2, t_r)]$$

referred to in (29). Subsequent projection onto the amplitude constraint set completes a single iteration of the POCS method, resulting in the next estimate  $\hat{f}_{\ell+1}(\cdot)$ .

One possible implementation of the POCS based reconstruction method is as follows:

1. Choose the reference image, and thus the reference time  $t_r$ .

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2. Specify the high resolution lattice, and determine the ratio between the density of the high resolution lattice and the lower resolution rectangular lattice over which the image values are generated via bilinear interpolation for motion estimation purposes. We refer to this ratio as  $r$ . (For instance,  $r=2$  in the examples given in Figs. 2 and 6.)

3. Perform motion estimation: spatially bilinearly interpolate each lower resolution image  $g(m_1, m_2, k)$  to lower resolution rectangular lattice; estimate motion from each interpolated lower resolution image, to the interpolated lower resolution image at  $t_r$ ; scale estimated motion vectors by  $r$ .

4. Define sets  $C_r(m_1, m_2, k)$  according to (24), for each pixel site  $(m_1, m_2, k)$  where the motion path is valid.

5. Compute the combined blur PSF

$$h_{t_r}(n_1, n_2, m_1, m_2, k)$$

for every site  $(m_1, m_2, k)$  where the sets

$$C_{t_r}(m_1, m_2, k)$$

have been defined.

6. Set

$$\hat{f}_0(n_1, n_2, t_r)$$

equal to the lower resolution image that has the best visual quality, after bilinearly interpolating it over the sampling lattice of the high resolution image.

7. For all sites  $(m_1, m_2, k)$  where the sets

$$C_{t_r}(m_1, m_2, k)$$

have been defined: compute the residual

$$r(\hat{f}_t)(m_1, m_2, k)$$

according to (25); back-project the residual

$$r(\hat{f}_t)(m_1, m_2, k)$$

using the projection

$$P_{t_r}(m_1, m_2, k)$$

in (26).

8. Perform the amplitude projection  $P_A$  using (28).

9. If the stopping criterion is satisfied then stop, otherwise go to Step 7.

After the stopping criteria is satisfied, the image may then be displayed, stored for future display, or transmitted for remote display.

The invention has been described with reference to a preferred embodiment. However, it will be appreciated that variations and modifications can be effected by a person of ordinary skill in the art without departing from the scope of the invention.

## Parts List:

- |    |                                     |
|----|-------------------------------------|
| 10 | lower resolution images             |
| 12 | provide mapping transformation step |

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14	compute combined PSF step
16	create high resolution image step
18	display high resolution image step
20	video camcorder/VCR
5 22	digitizer
24	digital still camera
26	digital video camcorder
28	digital scanner
30	disc stroage
10 32	image processing computer system
34	computer
36	CRT
38	keyboard
40	printer
15 42	storage medium
44	communication network
46, 48, 50	low resolution images
52	region of interest
53	low resolution image
20 54	diamond shaped sampling lattice
56	rectangular sampling lattice
60	optical system blur model
62	aperture time model
64	low resolution sampling model
25 66	additive noise model
68	sensor aperture
69	high resolution sampling regions
70	image
71	area swept by sensor aperture
30 73	center of sensor aperture
76	starting point
78	line
80	end point
82	center of region
35 84	transformed blur kernel
86	transformed blur kernel
88	high resolution image
90	low resolution image pixel

## Claims

1. A method for creating a high resolution image from a sequence of lower resolution motion images (10), comprising the steps of:
  - a. producing a mapping transformation (12) for each lower resolution image (10) to map pixels in each lower resolution image into locations in the high resolution image;
  - b. computing (14) a combined point spread function (PSF) for each pixel in each lower resolution image (10) employing the mapping transformations;
  - c. generating (16) the high resolution image from the lower resolution images employing the combined blur PSF by projection onto convex sets (POCS); and
  - d. displaying (18) the high resolution image.
2. The method claimed in claim 1, wherein the step of producing a mapping transformation includes:
  - a. selecting one of the lower resolution images as a reference image;
  - b. estimating a mapping transformation describing the relative motion at each pixel between the reference lower resolution image and each other lower resolution image;

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- c. testing the validity of the estimated mapping transformation for each other lower resolution image pixel and flagging valid mapping transformations; and
- d. scaling each valid mapping transformation from the lower resolution images to the high resolution image.

5 3. The method claimed in claim 1, wherein the step of computing a combined PSF includes:

- a. calculating an effective sampling aperture relative to the high resolution image for each pixel in each lower resolution image employing the mapping transformations;
- b. calculating PSF's for the effective sampling apertures;
- 10 c. defining an optical PSF; and
- d. combining the calculated PSF for each pixel with the optical PSF to produce the combined PSF for each pixel.

4. The method claimed in claim 1, wherein the step of generating the high resolution image by POCS includes:

- a. interpolating one of the lower resolution images to the number of pixels in the high resolution image to produce an estimate of the high resolution image; and
- b. for each pixel in each low resolution image having a valid mapping transformation, refining the estimate of the high resolution image by,

- i. selecting a pixel in one of the lower resolution images,
- ii. producing a calculated pixel value from the high resolution image by applying the combined PSF for the selected pixel to the current estimate of the high resolution image, and
- iii. forming the difference between the selected pixel value and the calculated pixel value and if the magnitude of the difference is greater than a predetermined threshold, back projecting the error into the current estimate of the high resolution image;

- c. clipping the pixel values of the refined estimate of the high resolution image to an allowable range; and
- d. repeating steps b and c until a stopping criterion is satisfied.

5. A method for producing a high resolution video sequence from a sequence of lower resolution video images, comprising applying the method claimed in claim 1 a plurality of times to the sequence of lower resolution video images to produce a video sequence of high resolution images.

6. Apparatus for creating a high resolution image from a sequence of lower resolution motion images, comprising:

- a. a source (20, 22, 24, 26, 28, 30) for producing a sequence of lower resolution motion images;
- b. an image processor (34, 36, 38) for receiving the sequence of lower resolution images and creating the high resolution image, including:

- i. means for producing a mapping transformation for each low resolution image to map pixels in each low resolution image into locations in the high resolution image;
- ii. means for computing a combined point spread function (PSF) for each pixel in each lower resolution image employing the mapping transformations;
- iii. means for generating the high resolution image from the lower resolution images employing the blur PSF's by projection onto convex sets (POCS); and

- c. a display device (40) for displaying the high resolution image.



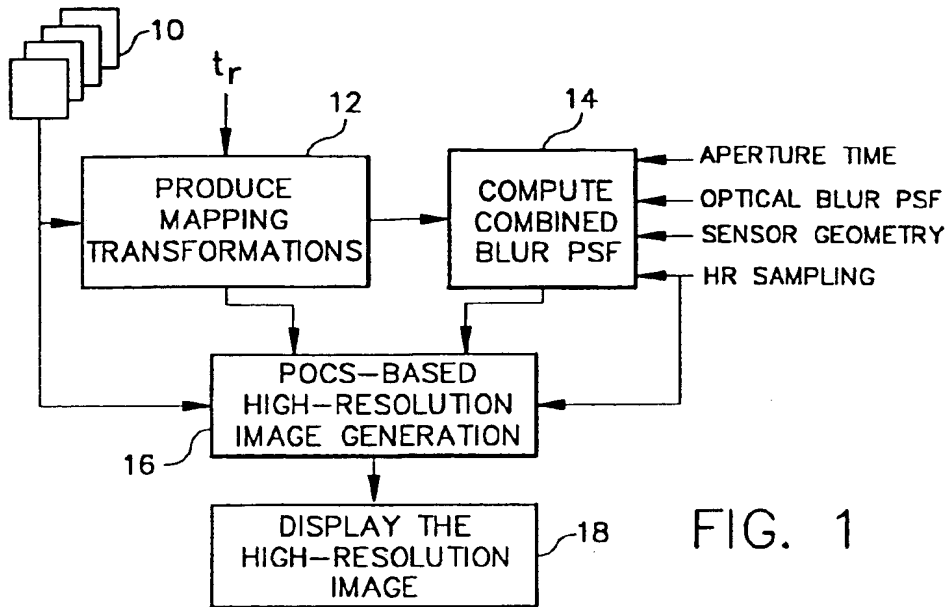


FIG. 1

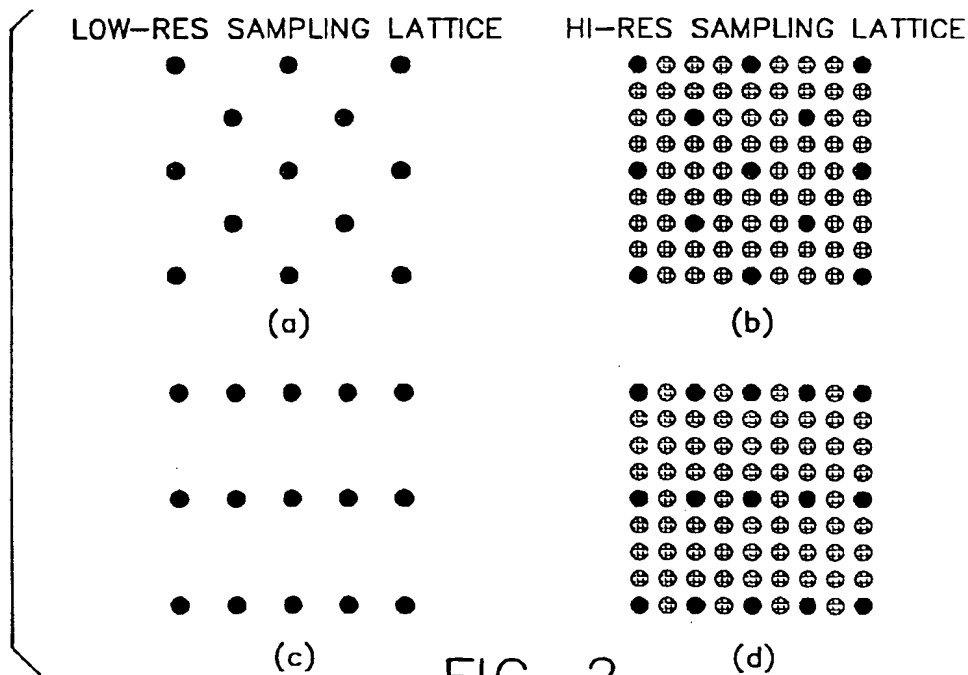


FIG. 2

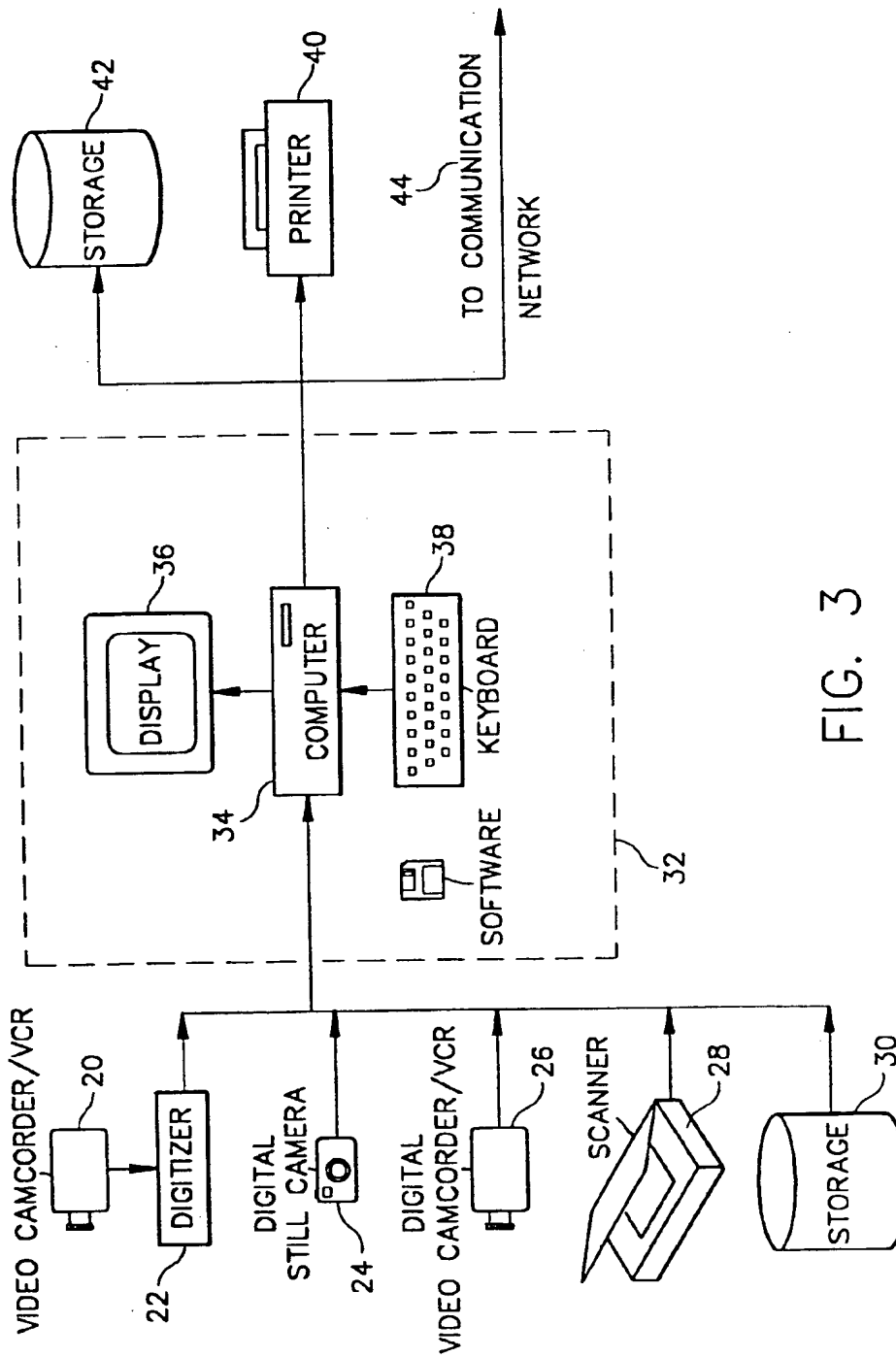


FIG. 3

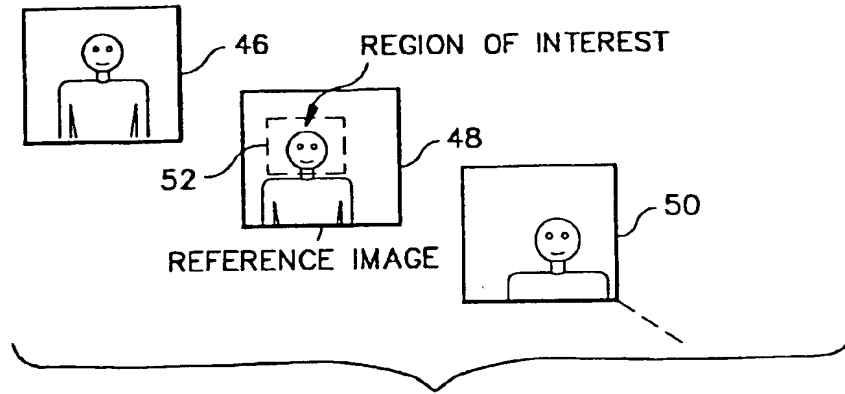


FIG. 4

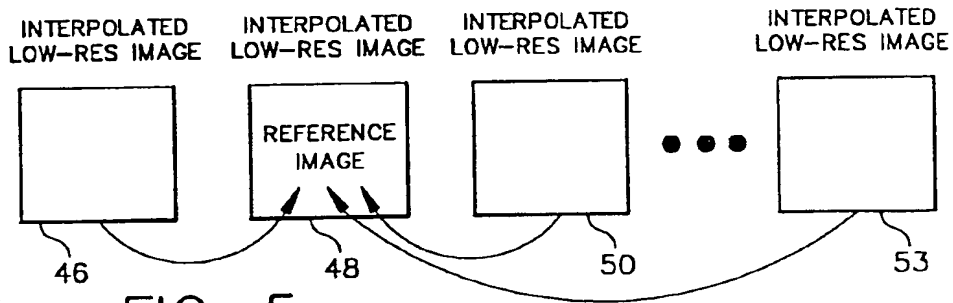


FIG. 5

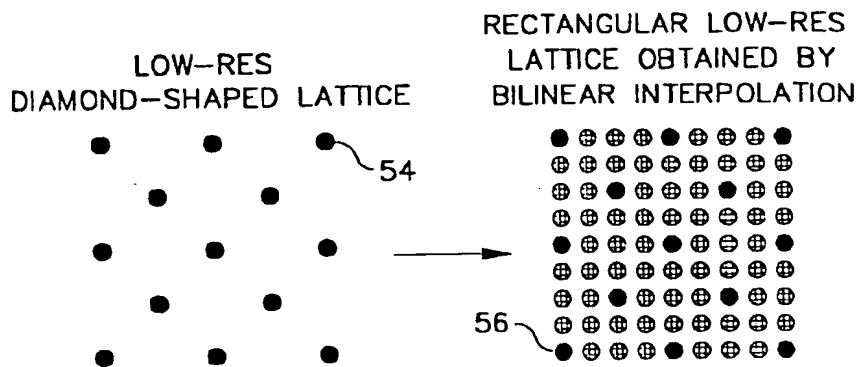


FIG. 6

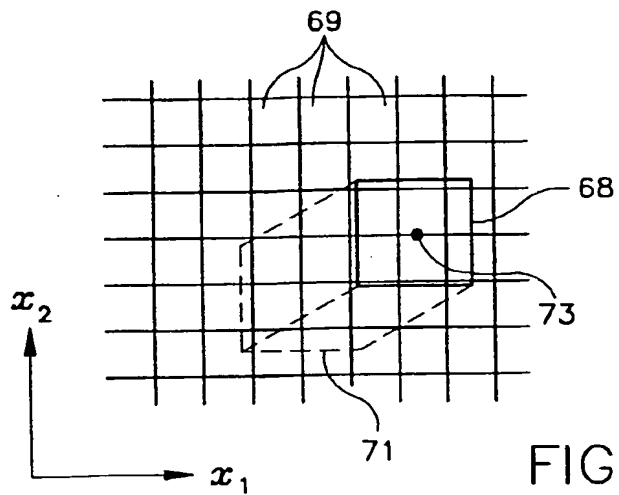


FIG. 9

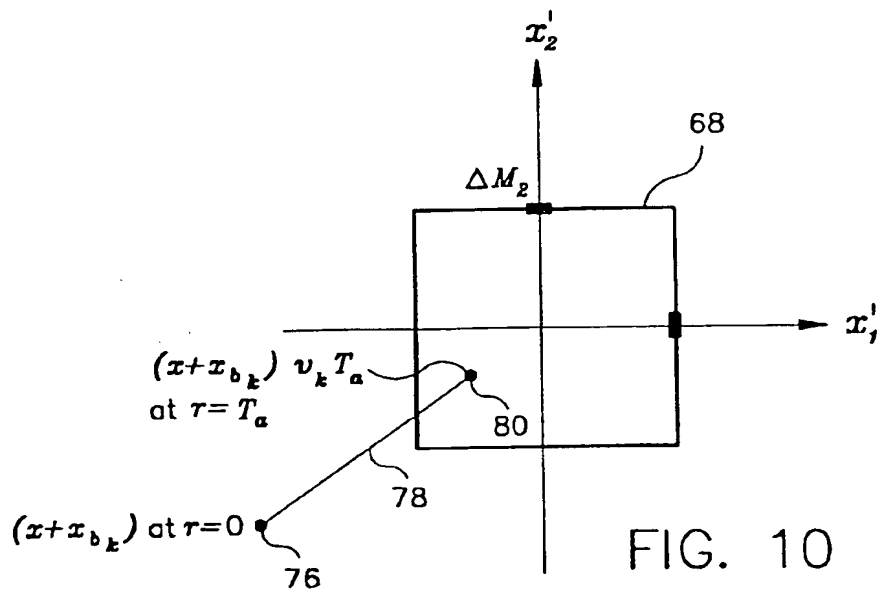


FIG. 10

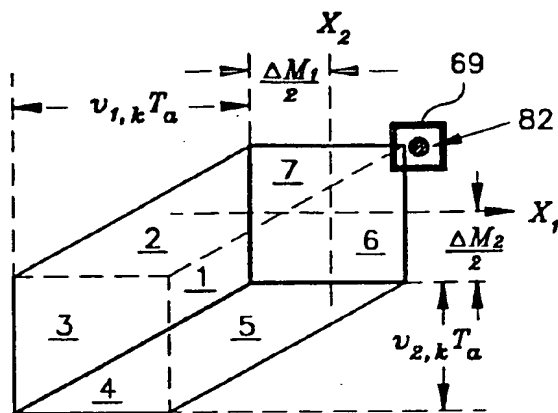


FIG. 11

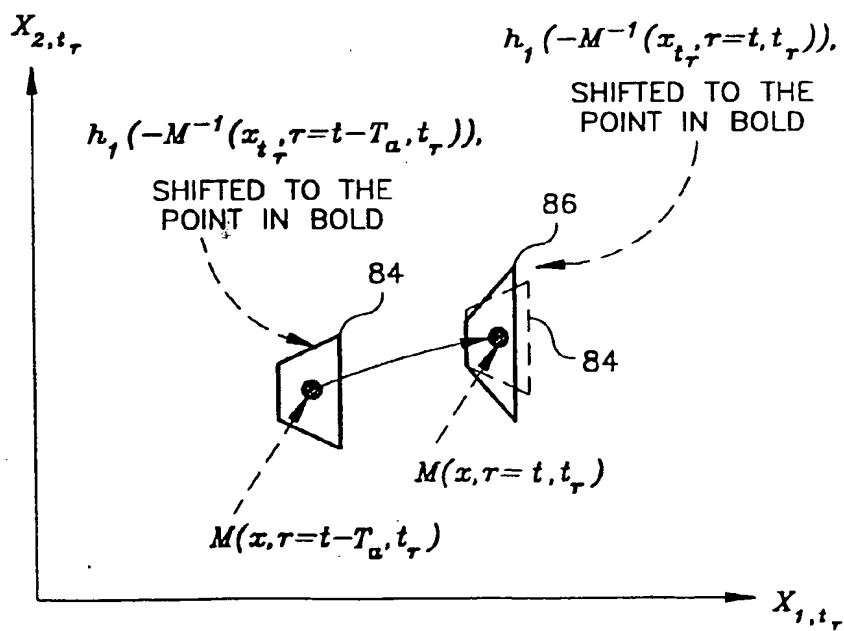


FIG. 12

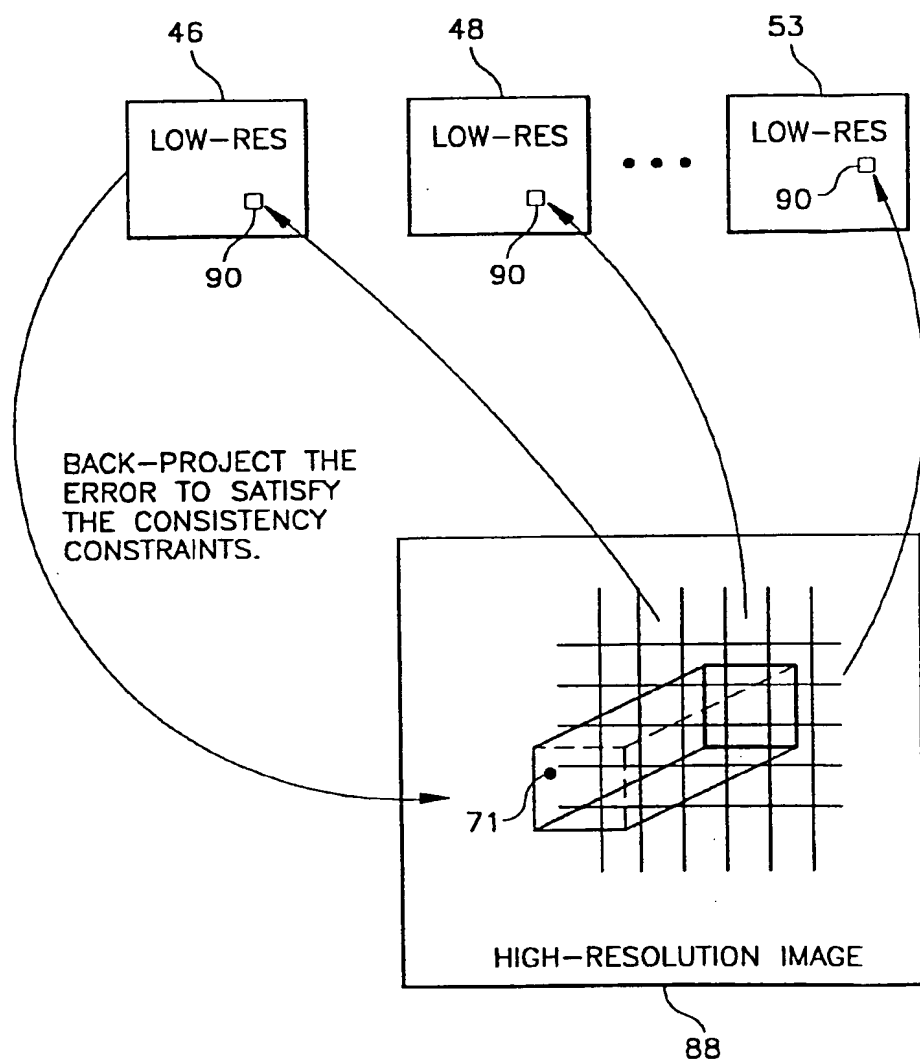


FIG. 13